

SUNDAY	MONDAY	TUESDAY	WEDNESDAY	THURSDAY	FRIDAY	SATURDAY
				<b>1</b> 國慶日 $57^{2016} \pmod{100} = ?$	<b>2</b> 二十 Find the square of the maximum value of $\sin x + \cos x$ .	<b>3</b> 廿一 3 is the first Cullen prime.
<b>4</b> 廿二 Let $S(x) = 1 + 2x + 3x^2 + \dots$ , find $S\left(\frac{1}{2}\right)$ .	<b>5</b> 廿三 5 is the smallest prime factor of 2015.	<b>6</b> 廿四 Today is the 184 <sup>th</sup> birthday of Richard Dedekind.	<b>7</b> 廿五 A 7-sided regular polygon cannot be constructed by compasses and straightedge.	<b>8</b> 寒露 Zenzizenzizic was a term coined by earlier mathematicians to indicate the 8 <sup>th</sup> power of a number.	<b>9</b> 廿七 $\frac{97524}{10836} = ?$	<b>10</b> 廿八 There are 10 types of people – those who understand binary and those who don't.
<b>11</b> 廿九 11 is the smallest Repunit prime.	<b>12</b> 三十 12 is the smallest abundant number.	<b>13</b> 九月 A cube has 13 axes of rotational symmetries.	<b>14</b> 初二 14 is the smallest positive integer $n$ such that $50n^2 + 1$ is a perfect square.	<b>15</b> 初三 $3n^5 + 5n^3 + 7n$ is divisible by 15 for all integers $n$ .	<b>16</b> 初四 It is known that $a, b, c$ are distinct and $\overline{abc}, \overline{acb}$ and $\overline{cba}$ are square numbers. Find $a + b + c$ .	<b>17</b> 初五 A 17-sided regular polygon can be constructed with compasses and straightedge.
<b>18</b> 初六 18 resembles the pronunciation of “will surely prosper” in Chinese	<b>19</b> 初七 $ABCD$ is a kite with perpendicular diagonals. If $AB = 16$ , $BC = 8$ and $CD = 13$ , find $DA$ .	<b>20</b> 初八 The number of quarter or half turns to solve a Rubik's Cube in worst case is 20.	<b>21</b> 重陽節 What is the fewest number of distinct integer-sided squares needed to tile a square?	<b>22</b> 初十 22 is the smallest positive integer which can be expressed as the sum of 2 primes in 3 ways.	<b>23</b> 十一 23 is the first prime number that its unique factorisation of cyclotomic integers based on the $p^{\text{th}}$ root of unity breaks down.	<b>24</b> 霜降 A tesseract has 24 two-dimensional faces.
<b>25</b> 十三 Today is the 204 <sup>th</sup> birthday of Évariste Galois.	<b>26</b> 十四 Today is the 104 <sup>th</sup> birthday of Chern Shiing-shen.	<b>27</b> 十五 27 is the largest number in the Platonic lambda series.	<b>28</b> 十六 28 is the second smallest perfect number, i.e. a number whose sum of divisors equals twice itself.	<b>29</b> 十七 If we write each date in the ddmyyyy format, how many palindromic dates are there in the 21 <sup>st</sup> century?	<b>30</b> 十八 The integer closest to $\pi^3 - \frac{\pi}{500}$ .	<b>31</b> 十九 Today is the 200 <sup>th</sup> birthday of Karl Weierstrass.



第五十七屆國際數學奧林匹克  
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